



HAL
open science

Electrical transport properties and modelling of electrostrictive resonance phenomena in Ba $2/3$ Sr $1/3$ TiO 3 thin films

Areski Ghalem, Laure Huitema, Aurelian Crunteanu, Mohamad Rammal, Lucian Trupina, Liviu Nedelcu, Gabriel Banciu, Perrine Dutheil, Catalin Constantinescu, Pascal Marchet, et al.

► To cite this version:

Areski Ghalem, Laure Huitema, Aurelian Crunteanu, Mohamad Rammal, Lucian Trupina, et al.. Electrical transport properties and modelling of electrostrictive resonance phenomena in Ba $2/3$ Sr $1/3$ TiO 3 thin films. *Journal of Applied Physics*, 2016, 120 (18), pp.184101-1-9. 10.1063/1.4966942 . hal-01394847

HAL Id: hal-01394847

<https://unilim.hal.science/hal-01394847>

Submitted on 10 Nov 2016

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Electrical transport properties and modelling of electrostrictive resonance phenomena in

$Ba_{2/3}Sr_{1/3}TiO_3$ thin films

A. Ghalem,^{1(*)} L. Huitema,¹ A. Crunteanu,¹ M. Rammal¹, L. Trupina²,
L. Nedelcu², M.G. Banciu², P. Dutheil³, C. Constantinescu³, P. Marchet³,
F. Dumas-Bouchiat³, C. Champeaux³

¹ XLIM UMR 7252 CNRS/ University of Limoges, 87060 Limoges, France.

² National Institute of Materials Physics, 077125 Bucharest-Magurele, Romania.

³ University of Limoges, CNRS, SPCTS, UMR 7315, F-87068 Limoges, France.

***Corresponding author:** Areski GHALEM

E-mail address: areski.ghalem@unilim.fr

Keywords: Ferroelectrics, BST, Conduction mechanisms, Electrostrictive resonances, Interface layer

ABSTRACT

We present the conduction mechanisms of $Ba_{2/3}Sr_{1/3}TiO_3$ thin films integrated in metal-insulator-metal (MIM) capacitors and the modelling of the frequency-dependent electrostrictive resonances (in the 100 MHz -10 GHz domain) induced in the devices upon applying different voltage biases. Au/BST/Ir MIM structures on MgO substrates have been fabricated and, depending on their specific polarization, we highlighted different conduction mechanisms in the devices. Depending on the dc bias polarity, the conduction current across the material shows a space-charge-limited-current behavior under negative polarization, while under positive bias the conduction obeys an electrode-limited Schottky-type law at the Au/BST interface.

The application of an electric field on the device induces the onset of acoustic resonances related to electrostrictive phenomena in the ferroelectric material. We modeled these acoustic

resonances over a wide frequency range, by using a modified Lakin model which takes into account the dispersions of acoustic properties near the lower electrode/ thin film interface.

I. INTRODUCTION

$\text{Ba}_x\text{Sr}_{1-x}\text{TiO}_3$ (BST) thin films are receiving considerable consideration as high-potential solutions for the conception of tunable devices in the microwaves and even the millimeter-waves¹⁻⁷. When integrated in capacitive metal-insulator-metal (MIM) structures, BST films are changing their permittivity upon application of a DC electric field, resulting in the modification of the overall capacitance of the MIM device with ratios up to 5:1⁸. Different ferroelectric thin layer compositions have been studied in detail⁹⁻¹¹. These barium contents can impose a specific state of the BST material (in ferroelectric or paraelectric forms) at room temperature.

The research presented in this paper (electrical and high-frequency characterization of BST material integrated in tunable MIM-type varactor devices) is a necessary step for the integration of the presented components in compact and low power consumption high-frequency devices. The final and specific goal is to realize a reconfigurable antenna exploiting the agility of BST materials integrated in MIM devices. The integration of a tunable BST-based capacitance within an antenna will reconfigure its working frequency for wireless communication on the ISM band going from 2.4GHz to 2.5GHz. To be competitive with other tunable components such as AsGa varactor diodes, the BST capacitors need to have low losses while having a good tunability and reliability¹²⁻¹⁴. Two factors are directly influencing both the BST losses and reliability: leakage currents of the MIM capacitances and the onset acoustic resonances at high frequencies. The global understanding and characterisation of these two phenomena are important and necessary steps for improving the quality of the BST

layer in order to obtain the best adapted capacitance value of the devices on the ISM band and, at the same time, the lowest losses in the same frequency band.

Depending on the electrode's type (noble metals, rutile-type oxides or complex perovskite oxides like LaNiO_3 or SrRuO_3 ¹⁵⁻¹⁷, typical conduction mechanisms proposed for BST thin film capacitors include film/electrodes interface- dominated Schottky emission¹⁸ bulk-related mechanisms like space-charge-limited conduction (SCLC)¹⁶ or Poole-Frenkel conduction²⁰ etc. For MIM capacitive structures, the electrode nature is therefore influencing the properties of the devices. Moreover, a variation of both lattice parameter and thermal expansion coefficient between the electrode and the film can cause important variations of dielectric properties and increase significantly leakage current^{21, 22}. Thus, interfacial layers between electrodes (the upper and/or the lower one) and the BST film have a significant impact on the degradation of dielectric BST thin film²⁰. The reason of this degradation can be explain by the bias drop across the interface, due to the occurrence of a depolarizing field near the electrodes. Indeed, when a dielectric material is submitted to an external electric field, the dipoles induced in the material generate a depolarizing electric field, which tends to oppose the external field and thus contributes to the fall of the polarization at the interfaces²⁴⁻²⁶. Consequently, the interfacial layer shows a much lower permittivity than the rest of the film and can be considered as a series parasitic capacitance, which may greatly reduce the material permittivity and therefore the capacitance of the BST device.

Besides the onset of leakage currents, an acoustic phenomenon occurs when applying DC bias voltages for tuning the BST permittivity within MIM structures. The magnitude of the applied electric fields breaks the central symmetry of the crystal and induces acoustic-type resonance phenomena²⁷⁻³⁰ which are a combination of electrostrictive and piezoelectric effects³¹⁻³⁴. These bias-induced electrostrictive phenomena are resulting in non-linear effects such as instabilities of the device capacitance and increased losses at specific resonant

frequencies in the microwave domain. Although these acoustic resonance phenomena can be appropriately used to develop voltage controlled resonators or filters^{35, 36} they may become easily a critical issue for high-frequency applications where losses, stability and linearity of the agile capacitors are essential.

A better understanding of this phenomenon on a wide frequency range (especially at microwave frequencies) requires to take into account various material properties (thicknesses, permittivity, acoustic velocities and impedances, etc.), as well as device designs (type of electrodes, electrode/ BST film interfaces, etc.). Lakin et al³⁷ developed a convenient analysis of these acoustic resonances induced by polarization fields. The model is using the electrical impedance description of each layer of the ferroelectric MIM capacitance considered as a parallel plate composite resonator. However, so far, the modeling of such acoustic phenomena was performed only for the first acoustic resonance appearing in the device response corresponding to a limited frequency domain³⁸.

The present paper focuses on transport properties and mechanisms for leakage current of asymmetric Au/ Ba_{2/3}St_{1/3}TiO₃/ Ir ferroelectric capacitors as well on the broad frequency band modelling of their electrostrictive behavior at different applied biases. Although there is a significant number of results concerning the electrical properties of the Pt / BST interface³⁹⁻⁴³, the electrical properties of the Ir/ BST system (Ir as bottom electrode) are less described in the literature^{14, 44}.

We also demonstrate, that the interfacial Ir electrode/ BST film layer plays a fundamental role within the Lakin formalism for properly model the additional secondary harmonic acoustic resonances of the electrostrictive responses in the MIM device, on a broader frequency domain.

II. EXPERIMENTAL PROCEDURE

In order to characterise the electrical transport properties of the BST layers, we fabricated MIM structures and evaluate their current-voltage (I-V) characteristics. The fabrication process starts with the deposition of an optimized iridium bottom electrode (100 nm) by radiofrequency magnetron reactive sputtering, at 600°C, on a MgO (100) substrate. It follows the deposition of the BST layer by pulsed laser deposition (PLD) from a $\text{Ba}_{2/3}\text{Sr}_{1/3}\text{TiO}_3$ target using a KrF (248 nm) excimer laser with a pulse rate of 10 Hz and a fluence of 4.5 J/cm^2 . During deposition, the substrate was kept at 700°C in oxygen atmosphere (ambient pressure of 0.3 mbar). The deposition time varies between 30 and 60 min with a target-substrate distance of 5 cm, resulting in BST film thicknesses between 200 nm and 1450 nm. Following their deposition, the BST films were structured in square patterns ($100 \times 100 \mu\text{m}^2$) using a photolithography step and wet etching. A 200-nm thick gold (Au) electrode with 10-nm thick Ti adhesion layer was finally thermally evaporated and patterned by a lift-off process on the top of the BST patterns. The surface of facing top and bottom electrodes is $30 \mu\text{m} \times 30 \mu\text{m}$ and the typical topology of the obtained MIM devices is depicted in Fig. 1.

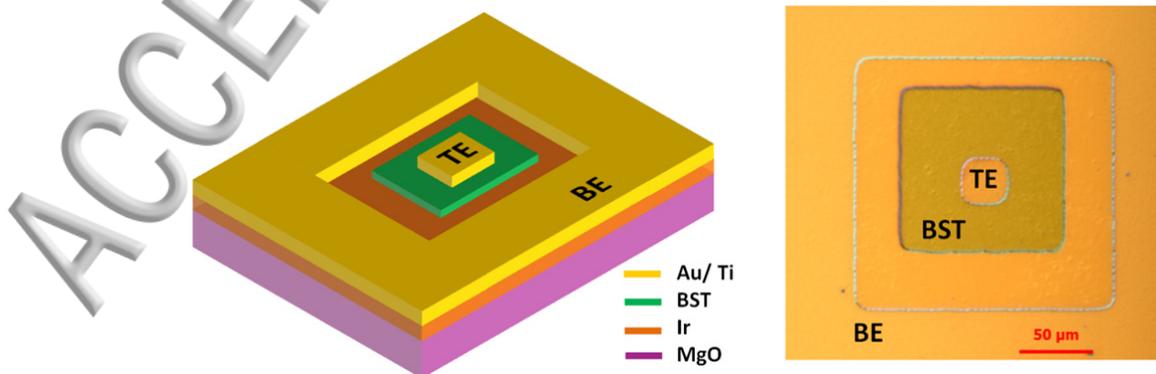


FIG.1. Schematic view of the fabricated MIM device and the associated optical microscopy top-view image. TE: top electrode, BE: bottom electrode.

DC and high-frequency characterization studies of the fabricated ferroelectric devices have been conducted at different temperatures and for different polarization voltages. The DC characterization allows extracting the current-voltage (I - V) characteristics of the MIM devices and was performed using a probe station connected to a Keithley 2612A sourcemeter. The device temperature was controlled using a Peltier module placed underneath. The response of the device in the high frequency domain (100 MHz- 10 GHz) was recorded using a Rohde & Schwarz vector network analyser (VNA) by measuring devices' reflection coefficient S_{11} (magnitude and phase) under different electrical fields applied between the top and the bottom electrodes (using a GSG (Ground-Signal-Ground) probe and an external bias Tee). For both the DC and RF measurements, the top gold (Au) electrode was biased either negatively or positively.

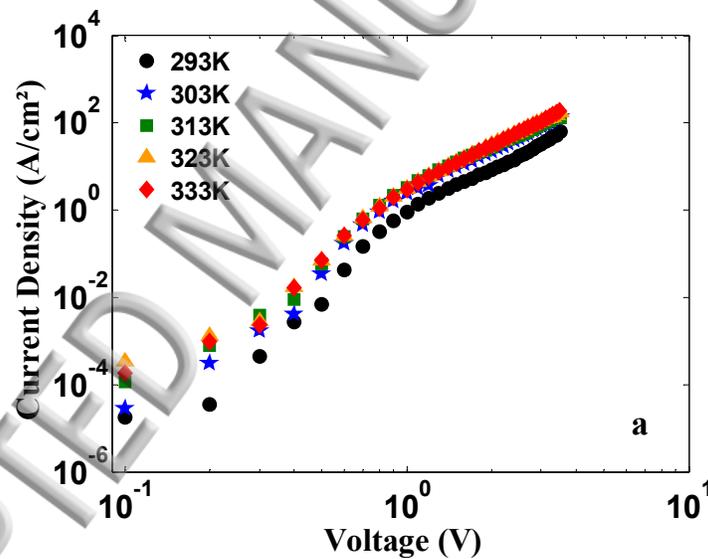
III. RESULTS AND DISCUSSION

A. DC electrical conduction mechanisms

The current density through the MIM device is defined as the ratio between the current and the square surface of facing electrodes can be deduced from the current-voltage measurements and plotted against the applied voltage. The interpretation of current density results reveals specific conduction mechanisms between metal (electrodes) and insulator (BST) which are directly linked to the metal/ insulator contact: neutral, blocking or ohmic. In this framework, two main conduction mechanisms can be distinguished: the conduction mechanism limited by electrodes/ film interfaces and the bulk limited conduction mechanism. The first one drives the conduction when the metal/ insulator contact is either neutral or blocking while the second one is observed for ohmic contacts.

The log-log current density as a function of the applied voltage characteristics have been obtained for I-V measurements performed on a 450 nm-thick BST MIM device, for temperatures and DC bias voltages ranging between 293K and 333K and from -4V to 30V, respectively.

For negative bias voltages applied to the top Au electrode (with Ir electrode at 20V), Figure 2 (a) shows that the current density is rapidly increasing with the applied voltage. Since current values are limited by the sourcemeter to 1.5 mA (in order to avoid additional heating and current breakdown phenomena in the thin film due to high leakage currents), the value of -4V is the lowest applied voltage which could be measured.



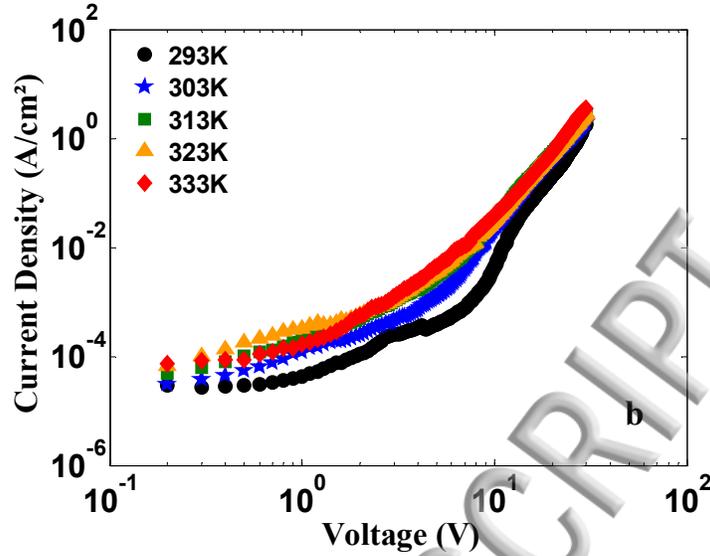


FIG. 2. Log-log representation of current density as a function of bias voltage applied to the top Au electrode for (a) negative and (b) positive bias voltages.

In this case, the bias voltage evolution and the temperature dependence can be related to a conduction mechanism limited by the interfaces and particularly to a Schottky emission mechanism¹⁸. Indeed, the Schottky effect corresponds to an injection of charges in the dielectric by passing above the potential barrier represented by the interface⁴⁵. In this case, the current density follows a temperature and electrical field evolution described by the equation (1).

$$J = A^* T^2 \exp \left[-\frac{q}{kT} \left(\phi_B^0 - \sqrt{\frac{qE}{4\pi\epsilon_0\epsilon_r}} \right) \right] \quad (1)$$

Where A^* is the Richardson's constant, T the temperature, $q\phi_B^0$ the potential barrier height, E the applied electric field and ϵ_r the relative dielectric permittivity of the BST material. The application of an electric field reduces the potential barrier and thus favours this type of charge injection.

The Schottky barrier is formed because the metal work function of gold electrode ($\Phi_{Au} = 5$ eV) is larger than the electron affinity of the BST film ($\chi_{BST} = 4.1$ eV). Consequently, in order to extract the apparent potential barrier at the BST (450 nm)/ Au interface, a Schottky mechanism can be considered in the case where the applied bias voltage on the MIM device is negative. The equation (1) can be also expressed as follows:

$$\ln\left(\frac{J}{T^2}\right) = \ln(A^*) - \frac{q}{kT} \phi_{app} \quad (2)$$

Where $q\Phi_{app}$ is the apparent barrier height, defined according to the equation (3):

$$\phi_{app} = \phi_B^0 - \sqrt{\frac{qE}{4\pi\epsilon_0\epsilon_r}} \quad (3)$$

The apparent barrier height can be calculated with the slope of the $\ln(J/T^2)$ versus $1000/T$ representation which is plotted on Figure 3 for different bias voltages. These plots are reasonably linear in the investigated temperature domain.

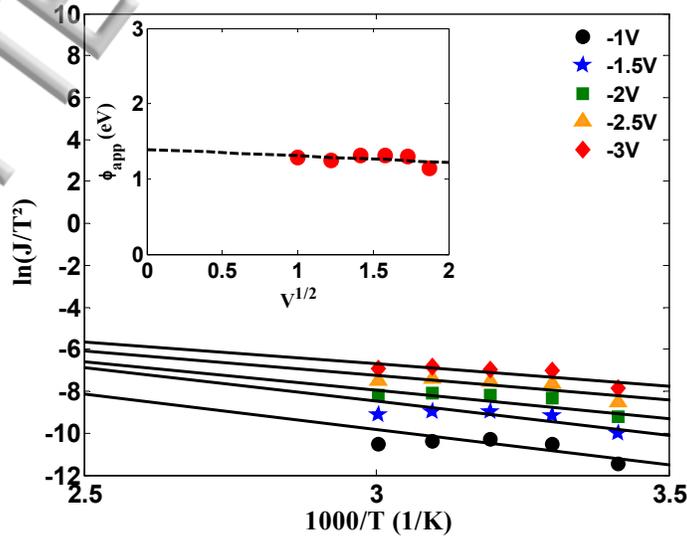


FIG. 3. $\ln(J/T^2)$ representation as the function of $1000/T$ for different negative bias voltages; inset: Evolution of activation energy as a function of DC bias.

The Schottky barrier height is the energy difference between the metal work function of Au and the electron affinity of the BST film and corresponds to the height of barrier that have to cross the charges when passing into the dielectric. It can be obtained by extrapolating the electric field to zero in the description of the apparent barrier height. The dependence of the apparent barrier height on $V^{1/2}$ is represented in the inset of Figure 3.

The extrapolation of the $\Phi_{app} = f(V^{1/2})$ at $V^{1/2} = 0$ allows to extract the Schottky barrier height, with a value of 1.39 eV at the BST/Au interface. This value is in agreement with previous results on similar systems⁴⁶.

The current-voltage evolution is different for a positive polarization (top Au electrode at positive bias and bottom Ir electrode at 0V, Figure 2-b). A different conduction mechanism may be clearly noted and the Figure 4 describes the log-log evolution of the current density as a function of the positive electric field for a MIM device integrating a 450-nm BST thick film, at 303 K. We observe that for a low bias voltage, the leakage current densities were below 4×10^{-4} A/cm² and the conduction mechanism is ohmic (slope = 1 on Figure 4). Between 3.5 V and 5.5 V, we clearly observe a transition to slope values greater than 1, reflecting a non-ohmic region. Under higher voltages, the log J-log V curve slopes are equal or greater than 2 and define a bulk-type conduction regime which agrees well with the Space Charge Limited Current – (SCLC) with deep traps mechanism^{18, 47}.

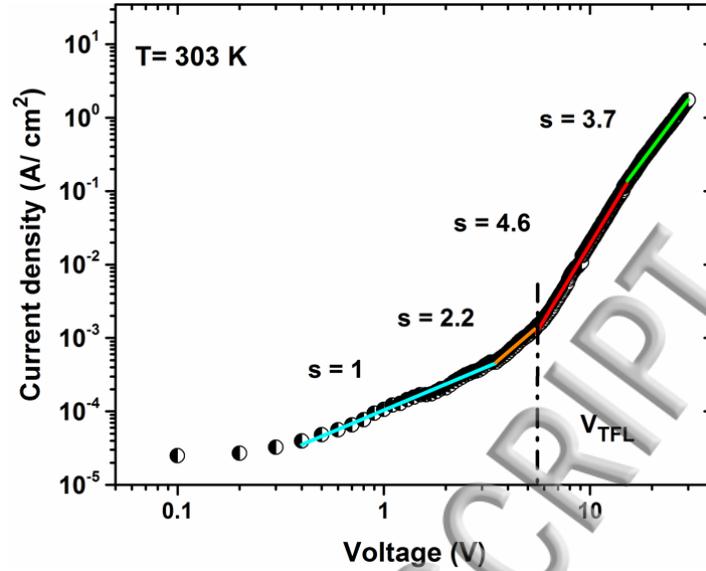


FIG. 4. Log-log plot of the current density vs the positive bias voltage for the MIM device integrating a 450-nm thick BST film, at 303 K.

Indeed, the SCLC theory describes the density current evolution according to the electric field by the relation ⁴⁸:

$$J = \frac{9\mu\epsilon_0\epsilon_r\theta \cdot E^2}{8d} \quad (4)$$

Where ϵ_r is the relative permittivity of the material, ϵ_0 the permittivity of the free space, μ the mobility, θ the ratio of free-to trapped electric charges and d the film thickness.

At low bias voltages, the injected carrier density is negligible compared to the intrinsic carrier density and the conduction is ohmic (slope equal to 1 in the J-V log-log representation on Figure 4). The SCLC regime occurs when the concentration of the built-in space charge cloud near the injected electrode is negligible against the injected charge density. The current density is following an E^2 dependence described by the equation 4 (slope around 2 in the log-log characteristics).

As the electric field increases up to a voltage threshold (the trap-free voltage limit (V_{TFL})), the amount of the injected charges is increasing and the density of free carriers injected into the active region becomes larger than its intrinsic charge density. Above V_{TFL} all the trap levels are filled and the device enters in a different regime (trap-free SCLC or SCLC regime described by different trap level distributions)⁴⁷.

If we consider the case of discrete shallow defect levels within the ferroelectric material (for voltages up to V_{TFL}), the density N_t of the trapped charges can be expressed as:

$$N_t = \frac{9}{8q} \epsilon_r * \epsilon_0 \frac{V_{TFL}}{d^2} \quad (5)$$

Where q is the charge of electron and V_{TFL} can be experimentally deduced from Figure 4. The extracted value of V_{TFL} is 5.5 V corresponding to a N_t value of $1.7 * 10^{20} \text{ cm}^{-3}$ at 303 K, which is consistent with previous reports on similar materials⁴⁹.

The trap energy level E_t can be further extracted from the expression of the ratio between the density of free and trapped electrons, θ , which can be expressed as (6):

$$\theta = \frac{N_c \exp[(E_t - E_c)/kT]}{g * N_t} \quad (6)$$

Where N_c is the effective density of states in the conduction band, g is a degeneracy factor (~ 2), E_c the energy level of conduction band, k the Boltzmann constant and T the temperature (K). Assuming $N_c = 10^{21} / \text{cm}^3$ ^{14,18,50}, we obtain the position of the energy level of traps with respect to the conduction band energy level, $E_c - E_t = 0.16 \text{ eV}$, which is in the same order of magnitude with those reported previously⁴⁹.

Taking into account the conduction mechanisms inferred for both negative and positive polarizations, the proposed schematic energy band diagram of the Au/ BST/ Ir capacitor is presented on Figure 5.

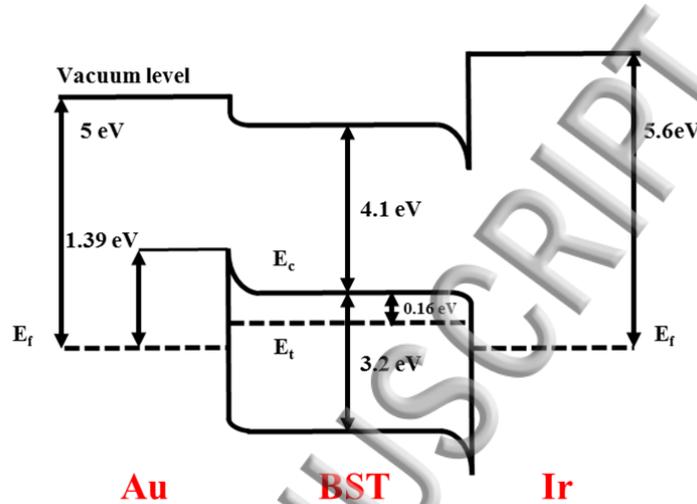


FIG. 5. Energy band diagram of the Au/BST/Ir capacitor.

We obtained similar results (analogous conduction mechanisms for an equivalent DC polarization) on MIM devices incorporating BST films with different thicknesses.

B. High-frequency characterization of the MIM devices

After analyzing the electrical characterization of BST thin films and the conduction phenomena at both metal-insulator interfaces, the next part of the paper will focus on the RF characterization of the BST thin films integrated in MIM tunable devices.

From the measurement of MIM devices reflection coefficients S_{11} (magnitude and phase) under different applied voltages, we can extract both the global capacitance and the resistance values⁵ according to equations 7 and 8, respectively.

$$C_{\text{meas}} = \frac{1}{Z_0 \cdot \omega \cdot \text{Im}\left(\frac{1+S_{11}}{1-S_{11}}\right)} \quad (7)$$

$$R_{\text{meas}} = \text{Re}(Z_{11}) = \text{Re}\left(Z_0 \cdot \frac{1+S_{11}}{1-S_{11}}\right) \quad (8)$$

The capacitance values variation with the electric field are plotted in Figure 6 for different thicknesses, of 200 nm, 450 nm and 1450 nm for the BST layer. Note that, the obtained films are highly oriented and exhibit a (100) preferred orientation with a small (111) contribution. Irrespective of the ferroelectric film thickness, the fabricated $\text{Ba}_{2/3}\text{Sr}_{1/3}\text{TiO}_3$ -based MIM devices show extremely high capacitance tuning. The relative capacitance variation goes up to 82% under an electric fields as low as 220 kV/cm which corresponds to an applied voltage of only 10V for the 450-nm thick MIM device.

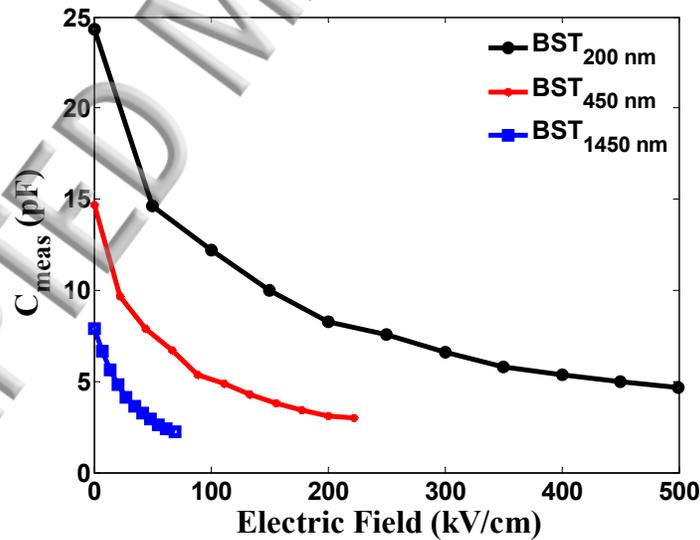


FIG. 6. Capacitance measurement as a function of electric field and for different thicknesses (maximum applied voltage bias of 10 V for all samples).

The state-of-the-art literature reports presented in the introduction section describes the relation between the degradation of both dielectric and acoustic properties of BST films with

the presence of an interface layer. This degradation, introduced by the electrode: ferroelectric film interface layer can be quantified by analysing its impact on the overall capacitance of the MIM device. Following the formalism used in ⁵¹, the capacitance measured for the MIM structure (C_{meas}) can be decomposed into the contribution of the BST film and that of the interfacial layer, according to the relationship (9):

$$\frac{1}{C_{\text{meas}}} = \frac{1}{C_f} + \frac{1}{C_i} \quad (9)$$

Where C_{meas} corresponds to the measured capacitance and equals $\frac{\epsilon_0 \epsilon_r S}{d}$ (S is the surface of the opposite electrodes and d the thickness of the BST layer) and C_i and C_f are the interface and ferroelectric layer capacitances, respectively. If the thickness of the global structure (d) is much higher than the one of the interface layer, it can be approximated to the ferroelectric film thickness, i.e. and the equation 9 becomes equivalent to the equation (10):

$$\frac{1}{C_{\text{meas}}} = \frac{d}{\epsilon_0 \epsilon_f S_f} + \frac{1}{C_i} \quad (10)$$

Therefore, the variation of the characteristic $1/C_{\text{meas}} = f(d)$ for MIM structures with different global thicknesses is a straight line whose slope is inversely proportional to the intrinsic dielectric permittivity of the ferroelectric layer, ϵ_f . The figure 7 describes the evolution of $1/C_{\text{meas}} = f(d)$ curve for BST films with different thicknesses of 200 nm, 450 nm and 1450 nm.

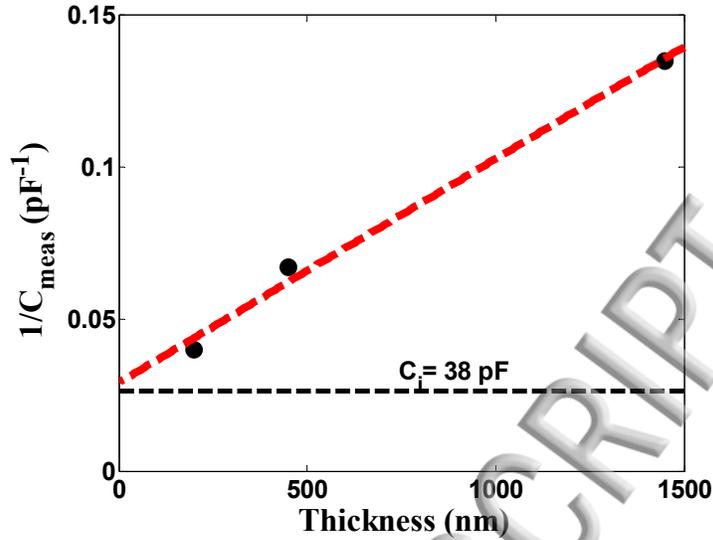


FIG. 7. Evolution of the inverse of capacitance ($1/C_{\text{meas}}$) as a function of BST film thicknesses.

The linear variation of the curve on Fig. 7 is in agreement with the series capacitance model that assumes the existence of regions with degraded dielectric properties close to the lower electrode/ferroelectric interface. Since $1/C_i$ is directly deduced from the y-intercept, we can calculate the interface capacitance, $C_i=38$ pF. Moreover, the intrinsic permittivity of the BST film (without the contribution of the interface layer) extracted from the slope is $\epsilon_f=2220$ and clearly exceeds the overall relative dielectric permittivity ϵ_r (around 1000) obtained by taking into account the contribution of the interface layer. We can therefore conclude that the interface between electrode and BST film contributes to the degradation of the dielectric properties and therefore cannot be disregarded when estimating the accurate dielectric properties of the ferroelectric material.

C. Modelling of the electrostrictive phenomena in the ferroelectric-based MIM device

Fig. 8 is plotting the measured overall resistance of the tunable device for the 450 nm-thick BST capacitor as a function of to the applied voltage. This resistance is equal to the real part of the device input impedance, Z_{11} , extracted from the measurement of reflection parameters S_{11} according to the equation 8. Curves on Fig. 8 are exhibiting the onset of acoustic-like

resonance effects when a DC-bias voltage is applied on the device, called electrostrictive resonances^{5, 49}. Therefore, the resistance values are corresponding to the global losses of the capacitor device, i.e. including BST film losses, electrodes losses and electrostrictive effects.

The electrostrictive resonances are reproducible and both their resonance frequencies and amplitudes are linked to the BST thickness⁸. Previous reports on these phenomena³³ shows that the main electrostrictive resonance is inversely proportional to the BST thickness. However, the knowledge on only the first resonance frequency is not sufficient for the integration of BST materials in practical devices like reconfigurable antennas or filters. Indeed, in the case presented Fig. 8, the fabricated tunable capacitance could be exploited only on the [3.8 GHz – 5.5 GHz] frequency range since outside this domain the overall losses are too high. The need to predict the onset and frequency domain of electrostrictive resonance effects is therefore necessary for practical device implementations.

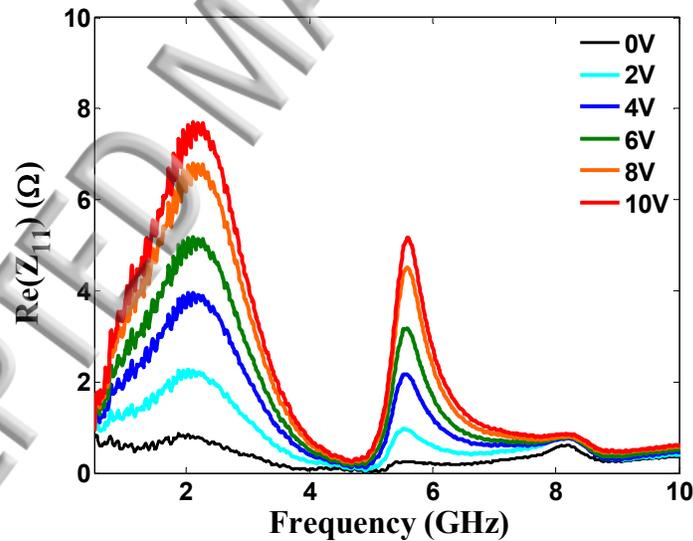


FIG. 8. Frequency evolution of the input impedance Z_{11} as a function of the bias voltage for MIM device integrating a 450-nm thick BST layer.

As indicated in the introduction part, the Lakin model^{53,54} is a simple and convenient approach for the simulation of acoustic/ electrostrictive behavior of ferroelectric layers integrating in MIM devices. The model is based on the acoustic transmission line

transformation by considering the acoustic properties of each constituent layers (substrate, electrodes, ferroelectric film). The electric impedance of the MIM capacitor is described by the normalized acoustic load impedances z_t and z_b on each side of the ferroelectric thin film sandwiched between the metallic electrodes (Fig.9).

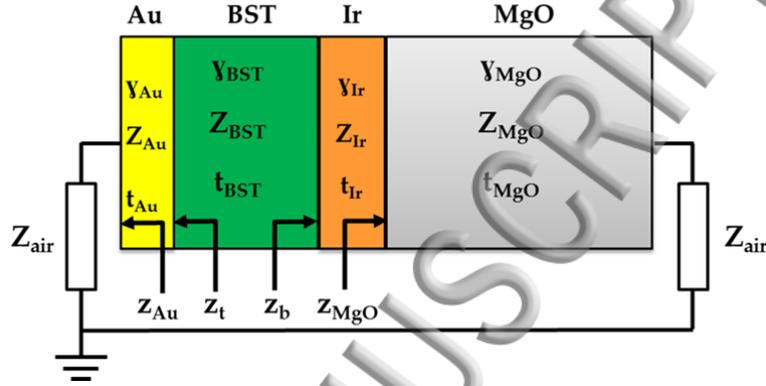


FIG. 9. Equivalent model of the ferroelectric MIM capacitor.

The equivalent acoustic impedance of the device is described by the equation (11):

$$Z_{eq} = \frac{1}{jC\omega} \left[1 - K^2(V_{DC}) * \frac{\tan \phi}{\phi} \left(\frac{(z_t + z_b) * \cos^2 \phi + j \sin(2\phi)}{(z_t + z_b) * \cos(2\phi) + j(z_t * z_b + 1) \sin(2\phi)} \right) \right] \quad (11)$$

where ω is the angular frequency, C is the global device capacitance, Φ is the phase over the BST layer defined as $\phi = k.t / 2$ with k the wave vector and t the BST thickness, $K^2(V_{DC})$ is the electromechanical coupling coefficient depending on the applied bias voltage V_{DC} , $z_t = Z_t/Z_{BST}$, $z_b = Z_b/Z_{BST}$, where, Z_{BST} is the acoustic impedance of the BST layer while Z_t and Z_b are the acoustic impedances of the top and bottom electrodes interfaces, respectively. Z_t and Z_b are calculating by using the classical transmission line equation (12):

$$Z_{interface} = Z_L \left(\frac{Z_i + Z_L \tanh(\gamma_i t_i)}{Z_L + Z_i \tanh(\gamma_i t_i)} \right) \quad (12)$$

$\gamma_i = \alpha_i + j\beta_i$, is the propagation constant for each layer within the structure, with α_i the attenuation constant and β_i the phase constant depending on the acoustic velocity, v_{ac} : $\beta_i = 2\pi f/v_{ac}$. Typical acoustic parameters for each layers composing the MIM device are described in Table 1.

Table 1. Geometrical and acoustic parameters of the layers considered in the MIM stack.

| Material | Thickness (μm) | v_{ac} (m/s) | $Z \cdot 10^6$ ($\text{kg/m}^2\text{s}$) |
|----------|-----------------------------|----------------|--|
| Au | 0.200 | 2200 | 62 |
| BST | 0.45 | 4400 | 55.1 |
| Ir | 0.100 | 3000 | 30 |
| MgO | 500 | 8000 | 28.6 |

The Lakin acoustic model has been implemented and the Fig. 10 is comparing the measurement and simulation results of the real part of the Z_{11} parameter for different applied DC bias voltage.

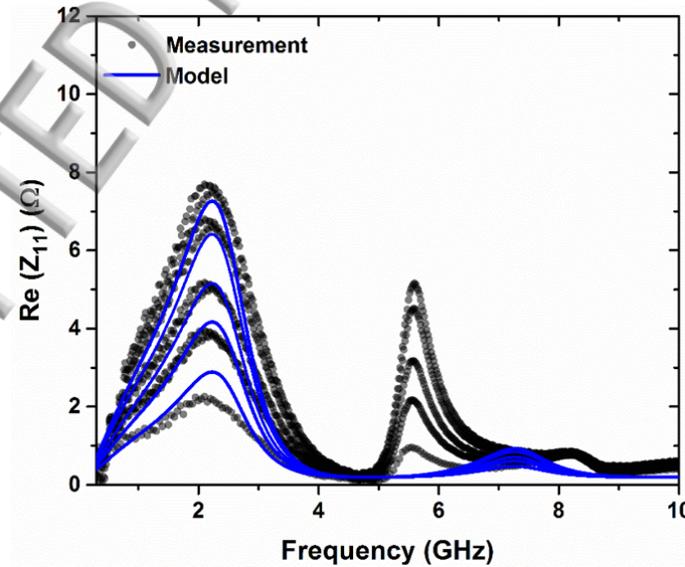


FIG. 10. Frequency evolution of the real part of the input impedance Z_{11} (modelled and measured) for different bias voltages.

As observed in Figure 10 and already confirmed for similar devices^{38, 41}, we noticed a good agreement between the implemented model and the experimental results for the main acoustic resonance peak, around 2.3 GHz. However, the current implementation of the model fails to correctly simulate the frequency position of the second acoustic harmonic which has a significant frequency shift and an important magnitude difference comparing with the measurement results. In order to explain this shift, *Vorobiev et al*⁵⁵ discussed the possibility of a frequency dispersion of the acoustic velocity in the ferroelectric material, which would explain in their case the frequency position of the second harmonic resonance.

Following this hypothesis, we further considered the introduction of an interfacial layer (typically about 10 - 70 nm) in the electrostrictive model layers stack at the Ir/ BST interface, with dissimilar acoustic properties in comparison with the main BST layer.

The different interpretations proposed in the literature consider this interfacial layer as a low permittivity medium and referred to is as an intrinsic layer^{56, 57}. Moreover, *Grossmann et al* and *Junquera et al*^{58,59} show a suppression of ferroelectric properties in $\text{Pb}(\text{Zr,Ti})\text{O}_3$ and BaTiO_3 thin film due to the presence of such interfacial layers. Based on the deterioration of the ferroelectric properties at the Ir/ BST interface, it is conceivable to consider also a modification of the acoustic properties of this interface layer.

Taking into account all these considerations, the previous electrostrictive model stack was modified (inset in Fig. 11) by introducing an interface layer with optimized acoustic properties (layer thickness of 50 nm with an acoustic velocity of 2200 m/s, around two times less than the acoustic velocity of BST thin films). The comparison of the measurement results and the modelled input impedance of the modified layers stack within the MIM capacitance are represented on Figure 11.

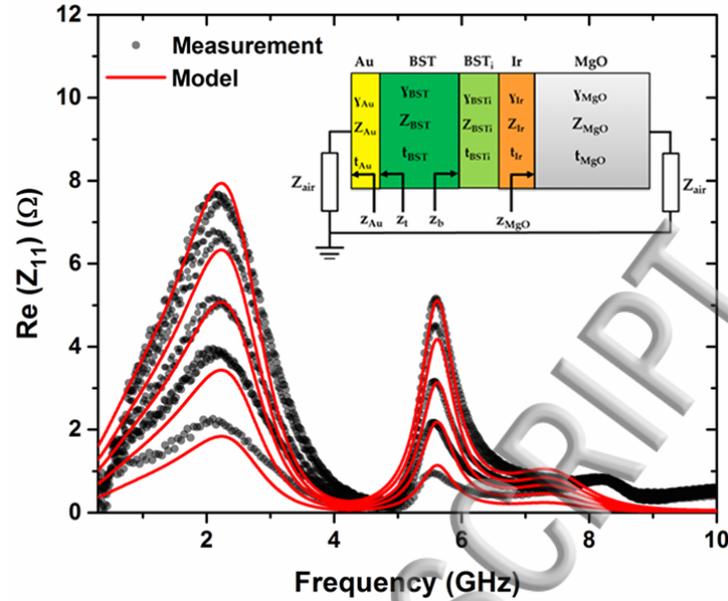


FIG. 11. Frequency evolution of the input impedance (modelled and measured) for different bias voltages considering an equivalent model of the MIM capacitor which is incorporating an Ir/ BST interface layer (inset).

It is obvious from the results presented in Figure 11 that by taking into account an interface layer at the Ir/BST boundary having specific acoustic properties, the electrostrictive resonances induced in the device can be modelled not only for the first resonance peak but also for the successive harmonics, on a larger frequency band.

These results are important from the point of view of predicting and evaluating the overall device losses on a larger frequency domain. Indeed, it should be remind that the real part of the Z_{11} parameter equals the equivalent resistance of the tunable capacitance. Within the radiating element of a tunable antenna, a resistance higher than 2Ω is not acceptable therefore the electrostrictive resonances (frequency positions and amplitude) need to be predicted in order to dismiss them from the working frequency band of the antenna.

The impact of this interfacial layer on the global acoustic properties of ferroelectric MIM devices is still not completely documented, and its real nature remains a subject of discussion in the domain. Nevertheless, different hypothesis have been proposed concerning its origin such as: (i) the destruction of the polarization states near the interface⁵⁴, ii) the formation of specific conduction mechanisms due to the difference in the band structure between the BST

layer and the electrode ^{18, 60} or (iii) a thin layer adjacent to the electrode with particular microstructure which behaves like a series capacitor ⁶¹.

The evaluation of the interface layer thickness using the electrostrictive model approach described above allows obtaining further information concerning the dielectric properties of this boundary layer.

In order to have a rough size of the permittivity near the interface, the thickness obtained from the electrostrictive effects simulation was reintroduced in the expressions defining the interface capacitance (eqs. 9 and 10). Indeed, from the curve on Figure 7 describing the variation of the BST measured capacitance ($1/C_{\text{meas}}$) as a function of the ferroelectric layers thicknesses we may extrapolate it and extract the Y-intercept of the curve which is defining the capacitance associated with the interface layer (eq. 13), which can be expressed as:

$$\frac{1}{C_i} = \frac{e_i}{\epsilon_0 \epsilon_i S_i} \quad (13)$$

Where C_i is the interface capacitance, e_i , ϵ_i and S_i are the thickness, the permittivity and the surface of the interface layer, respectively. Considering a value of $e_i = 50$ nm, we obtained a permittivity value of $\epsilon_i \sim 240$ which is significantly lower than that of the BST film. As indicated in the previous section, such a small permittivity of the Ir/ BST interface layer affects greatly the overall dielectric properties of the ferroelectric BST thin film and the capacitance values of the MIM device. Nevertheless, these results confirm the assumptions concerning the nature of this interface layer, which is expected to have highly dissimilar dielectric properties compared to the ferroelectric film, with a very low permittivity and degraded acoustic and ferroelectric behavior ^{58, 62, 63}. The rigorous simulation of electrostrictive phenomena on a broad frequency domain of such metal/ferroelectric/metal structures must therefore take imperatively into account the influence of the lower electrode/ferroelectric film interface layer.

IV. CONCLUSION

In this paper, we studied the conduction mechanisms MIM devices integrating a paraelectric $\text{Ba}_{2/3}\text{Sr}_{1/3}\text{TiO}_3$ thin film with paraelectric behavior at room temperature. The negative and positive polarization of the device allowed determining the conduction laws (Schottky and SCLC, respectively) and the band diagram of the Au / BST / Ir / MgO structure. The analysis of the dielectric properties of the BST films along with the modeling of electrostrictive acoustic resonance phenomena appearing in the MIM devices in the high-frequencies domain indicate the existence of an interface layer at the BST/ Ir boundary with dissimilar dielectric and acoustic properties when compared with the BST layer. We demonstrate that the modification of the electrostrictive Lakin model by including this interface layer in the overall layer stack of the device shows an excellent agreement between the modeled and the measured results over a wide frequency range. The modelling results presented here are relevant from the device integration point of view, by predicting and evaluating the overall device losses on a large frequency domain.

V. ACKNOWLEDGEMENT

This work was financially supported by the “Agence Nationale de la Recherche” (ANR)-France and the National Authority for Scientific Research (ANCS)-Romania, under the project MAESTRO ANR-13-ISO3-001.

VI. REFERENCES

- ¹ S. Courrèges, B. Lacroix, A. Amadjikpe, S. Phillips, Z. Zhao, K. Choi, A. Hunt, J.Papapolymerou, "Back-to-back tunable ferroelectric resonator filters on flexible organic substrates." IEEE Transactions on Ultrasonics. Ferroelectrics and Frequency. Control, **57**, 2010.
- ² R.De Paolis, S.Payan, M. Maglione, G.Guegan, F.Cocchetti. "High-Tunability and High- Q - Factor Integrated Ferroelectric Circuits up to Millimeter Waves" IEEE Transaction Microwave Theory and Technique, **63**, 2015.
- ³ T.Kimura, H.Kobayashi, Y.Kishimoto, H.Kato, M.Inaba, K-Y.Hashimoto, T. Matsumura, H.Hirano, M.Kadota, M.Esashi, S.Tanaka. "S.Bandwidth-tunable filter consisting of SAW resonators and BaSrTiO₃ varactors directly fabricated on a LiTaO₃ wafer" IEEE International Ultrasonics Symposium (IUS), 2014.

- ⁴ I.Vendik, V.Pleskachev, E.Zameshaeva, P.Turalchuk, D.Kholodnyak, I.Kolmakova, S.Zubko, I.Munina, V.Turgaliev, M.Sitnikova, M.Odit, X.Wang, N.Li, L.Sun, Y.He. Proceedings of the 43rd European Microwave Conference, 2013.
- ⁵ G.Subramanyam, M-W.Cole, N-X.Sun, T-S.Kalkur, N-M.Sbrockey, G-S.Tompa, X.Guo, C.Chen, S-P.Alpay, G-A.Rossetti Jr., K.Dayal, L-Q.Chen, D-G.Schlom. “Challenges and opportunities for multi-functional oxide thin films for voltage tunable radio frequency/microwave components” Journal of Applied Physics, **114**, 191301, 2013.
- ⁶ H. Khassaf, N. Khakpash, F. Sun, N-M. Sbrockey, G-S. Tompa, T-S. Kalkur, S-P. Alpay. “Strain engineered barium strontium titanate for tunable thin film resonators” Applied Physics Letters, **104**, 202902, 2014.
- ⁷ N-M. Sbrockey, T-S. Kalkur, A. Mansour, H. Khassaf, H-Yu, M. Aindow, S-P. Alpay, G-S. Tompa “Switchable and tunable film bulk acoustic resonator fabricated using barium strontium titanate active layer and Ta₂O₅/SiO₂ acoustic reflector” Applied Physics Letters, **109**, 052902, 2014.
- ⁸ A.Ghalem, M.Rammal, L.Huitema, A. Crunteanu, V. Madrangeas, P. Dutheil, F. Dumas Bouchiat, P. Marchet, C. Champeaux, L. Trupina, L. Nedelcu, M.G. Banciu “Ultra-High tunability of Ba_(2/3)Sr_(1/3)TiO₃-based Capacitors under Low Electric Fields”. IEEE Microwave and Wireless Components Letters, **26**, pp 504-506, 2016.
- ⁹ H. S. Kim, H. G. Kim, I. D. Kim, K. B. Kim, and J. C. Lee, “High tunability and low-microwave-loss Ba_{0.6}Sr_{0.4}TiO₃ thin films grown on high-resistivity Si substrates using TiO₂ buffer layers,” Applied Physics Letters, **87**, 212903, 2005.
- ¹⁰ C. L. Chen, H. H. Feng, Z. Zhang, A. Brazdeikis, Z. J. Huang, W. K. Chu, C. W. Chu, F. A. Miranda, F. W. Van Keuls, R. R. Romanofsky, Y. Liou, “Epitaxial ferroelectric Ba_{0.5}Sr_{0.5}TiO₃ thin films for room-temperature tunable element applications,” Applied Physics Letters, **75**, no. 3, pp. 412–414, 1999.
- ¹¹ D. A. Boyd, S. G. Hirsch, C. Hubbard, and M. W. Cole, “BST films grown by metal organic chemical vapor deposition incorporating real-time control of stoichiometry,” Integr. Ferroelectr. **111**, no.1, pp. 17–26, 2009.
- ¹² D.Levasseur, H-B. El-Shaarawi, S. Pacchioni, A. Rousseau, S. Payan, G. Guegan, M. Maglione “Systematic investigation of the annealing temperature and composition effects on the dielectric properties of sol–gel Ba_xSr_{1-x}TiO₃ thin films” Journal of the European Ceramic Society, **33**, pp 139–146 2013.
- ¹³ W-Y. Hsu, J-D.Luttmer, R.Tsu, S.Summerfelt, M-Bedekar, T.Tokumoto, J.Nulman. “Direct current conduction properties of sputtered Pt/(Ba_{0.7}Sr_{0.3})TiO₃/Pt thin films capacitors” Applied physics letters, **66**, 2975, 1995.
- ¹⁴ C-S.Hwang, B-T.Lee, C-S.Kang, J-W.Kim, K-H.Lee, H-J.Cho, H.Horii, W-D.Kim, S-I.Lee, Y-B.Roh, M-Y.Lee. “A comparative study on the electrical conduction mechanisms of (Ba_{0.5}Sr_{0.5})TiO₃ thin films on Pt and IrO₂ electrodes” Journal of Applied Physics, **83**, 3703, 1998.

- ¹⁵ T.Kawakubo, S.Komatsu, K.Abe, K.Sano, N.Yanase, N.Fukushima “Ferroelectric Properties of SrRuO₃/(Ba, Sr)TiO₃/SrRuO₃ Epitaxial Capacitor “ Japanese Journal of Applied Physics, vol **37**, 1998.
- ¹⁶ A.Srivastava, D. Kumar, R.K.Singh, “LaNiO₃ as Contact Material for (Ba,Sr)TiO₃ Dielectric Thin Films” Electrochemical and Solid-State letters, **2**, pp 294-296, 1999.
- ¹⁷ Y-K.Reddy, J.Wolfman, M.Gervais, F.Gervais, “Frequency dependent negative capacitance of (Ba_{0.6}Sr_{0.4})(Zr_xTi_{1-x})O₃ thin films grown on La_{0.9}Sr_{1.1}NiO₄ buffered SrTiO₃ substrate” Materials Science, pp 1-4, 2009.
- ¹⁸ S-T.Chang, J-Y.Lee. “Electrical conduction mechanism in high-dielectric-constant (Ba_{0.5},Sr_{0.5})TiO₃ thin films” Applied physics letters, **80**, 655, 2002.
- ¹⁹ M-A. Khan, T-P. Comyn, A-J. Bell, “Deposition of PbTiO₃ films on Pt/Si substrates using pulsed laser deposition” Journal European Ceramic Society, **28**, 591, 2008.
- ²⁰ C-S.Hwang, “Bulk- or interface-limited electrical conduction in IrO₂/(Ba,Sr)TiO₃/IrO₂ thin film capacitors” Journal of Materials Research, **16**, pp 3476-3484, 2001.
- ²¹ T-M.Shaw, Z.Suo, M.Huang, E.Liniger, R-B.Laibowitz, J-D.Baniecki. “The effect of stress on the dielectric properties of barium strontium titanate thin films” Applied Physics letters, **75**, p 2129, 1999.
- ²² S-Y.Wang, B-L.Cheng, C.Wang, S-A.Redfern, S-Y.Dai, K-J.Jin, H-B.Lu, Y-L.Zhou, Z-H.Chen, G-Z.Yang, “Influence of Ce doping on leakage current in Ba_{0.5}Sr_{0.5}TiO₃ films ” Journal of Physics D: Applied Physics, **38**, pp 2253-2257, 2005.
- ²³ S-H. Paek, J.Won, K-S.Lee, J-S.Choi, C-S.Park, “Electrical and Microstructural Degradation with Decreasing Thickness of (Ba, Sr)TiO₃ Thin Films Deposited by RF Magnetron Sputtering” Japanese Journal of Applied Physics, **35**, 1996.
- ²⁴ Y.Wang, M-K.Niranjan, K.Janicka, J-P. Velev, M-Y.Zhuravlev, S-S.Jaswa, E-Y. Tsymbal. “Ferroelectric dead layer driven by a polar interface”. Physical Review B, **82**, 094114, 2010.
- ²⁵ N-A.Spaldin, “Fundamental Size Limits in Ferroelectricity” Science, **304**, 1606, 2004.
- ²⁶ R-R. Mehta, B-D. Silverman, J-T. Jacobs, “DC bias dependent shift of resonance frequencies in BST thin film membranes” IEEE International Symposium on the Applications of Ferroelectrics, pp 236-238, 2007.
- ²⁷ A. Noeth, T. Yamada, V. Sherman, P. Muralt, A. Tangantsev, N. Setter “Modeling tunable bulk acoustic resonators based on induced piezoelectric effect in BaTiO₃ and Ba_{0.25}Sr_{0.75}TiO₃ films”. Journal of Applied Physics, **103**, 2008.

- ²⁸ A. Vorobiev, S.Gevorgian, N.Martirosyan, M.Löffler, E.Olsson. “Intrinsically tunable $0.67\text{BiFeO}_3\text{-}0.33\text{BaTiO}_3$ thin film bulk acoustic wave resonators” Applied Physics letters, vol **101**, p 232903, 2012.
- ²⁹ S. Gevorgian, A. Vorobiev, T. Lewin. “dc field and temperature dependent acoustic resonances in parallel-plate capacitors based on SrTiO_3 and $\text{Ba}_{0.25}\text{Sr}_{0.75}\text{TiO}_3$ films: Experiment and modeling”. Journal of Applied Physics, **99**, 124112, 2006.
- ³⁰ A.Noeth, T.Yamada, A-K.Tagantsev, N.Setter. “Electrical tuning of dc bias induced acoustic resonances in paraelectric thin films capacitors”. Journal of Applied Physics, **104**, 094102, 2008.
- ³¹ S. Tappe, U. Bottger, and R. Waser, “Electrostrictive resonances in $\text{Ba}_{0.7}\text{Sr}_{0.3}\text{TiO}_3$ thin films at microwave frequencies” Applied Physics Letters, **85**, 624, 2004.
- ³² W-P. Mason, B-T.Matthias, “Theoretical Model for Explaining the Ferroelectric Effect in Barium Titanate” Physical Review , **74**, 1622, 1948.
- ³³ X. Zhu, J. D. Phillips, and A. Mortazawi, “A DC voltage dependent switchable thin film bulk wave acoustic resonator using ferroelectric thin film,” 2007 IEEE MTT-S Int. Microwave Symp. Dig., pp. 671–674, 2007.
- ³⁴ W-P. Mason, “An Electromechanical Representation of a Piezoelectric Crystal used as a Transducer” Proceedings of the Institute of Radio Engineers (IRE), **23**, pp 1252-1263, 1935.
- ³⁵ M. Schreiter, R. Gabl, D. Pitzer, R. Primig, W. Wersing, “Electro-acoustic hysteresis behaviour of PZT thin film bulk acoustic resonators”, Journal of European Ceramic Society, **24**, pp 1589-1592, 2004.
- ³⁶ P-B. Kirby, Q-X. Sua, E. Kornuroa, Q.Zhang, M.Imuraapb R-W. Whatmore, “PZT thin film bulk acoustic wave resonators and filters” IEEE International Frequency Control Symposium and PDA Exhibition, pp 687-694, 2001.
- ³⁷ K-M.Lakin, G-R.Kline, K-T Carron, “High-Q Microwave Acoustic Resonators and Filters” IEEE Transaction Microwave Theory Tech, **41**, pp 2139–2146, 1993.
- ³⁸ I.Vendik, P-A.Turalchuk, O-G.Vendik, J.Berge. “Modeling tunable bulk acoustic resonators based on induced piezoelectric effect in BaTiO_3 and $\text{Ba}_{0.25}\text{Sr}_{0.75}\text{TiO}_3$ films”. Journal of Applied Physics, **103**, 014107, 2008.
- ³⁹ A.Vorobiev, J.Berge, S.Gevorgian, M.Löffler, E.Olsson. “Effect of interface roughness on acoustic loss in tunable thin film bulk acoustic wave resonators” Journal of Applied Physics, **110**, 024116, 2011.
- ⁴⁰ D Levasseur, E Bouyssou, R De Paolis, A Rousseau, F Coccetti, G Guegan, S Payan and M Maglione “Systematic tuning of the conduction mechanisms in ferroelectric thin films” Journal of Physics: Condensed Matter, **25**, 2013.

- ⁴¹ B.Ivira, A.Reinhardt, E.Defay, M.Aid. “Integration of electrostrictive $Ba_{0.7}Sr_{0.3}TiO_3$ thin films into Bulk Acoustic Wave resonator for RF-frequency tuning under DC bias” IEEE International Frequency Control Symposium, pp 254-258, 2008.
- ⁴² A-G.Altynnikov, A-G.Gagarin, M-M.Gaidukov, A.Tumarkin, P-K.Petrov, N. Alford, A-B. Kozyrev. “Suppression of slow capacitance relaxation phenomenon in Pt/ $Ba_{0.3}Sr_{0.7}TiO_3$ /Pt thin film ferroelectric structures by annealing in oxygen atmosphere” Applied physics letters, **104**, 042903, 2014.
- ⁴³ W-Y. Hsu, J-D.Luttmer, R.Tsu, S.Summerfelt, M-Bedekar, T.Tokumoto, J.Nulman. “Direct current conduction properties of sputtered Pt/ $(Ba_{0.7}Sr_{0.3})TiO_3$ /Pt thin films capacitors” Applied physics letters, **66**, 2975, 1995.
- ⁴⁴ B.Mešić, H.Schroeder “Integration of perovskite oxide dielectrics into complementary metal–oxide–semiconductor capacitor structures using amorphous TaSiN as oxygen diffusion barrier” Journal of Applied Physics, **110**, 064117, 2011.
- ⁴⁵ L.Pintilie, I. Vrejoiu, D. Hesse, G. LeRhun, M. Alexe. “Ferroelectric polarization-leakage current relation in high quality epitaxial $Pb(Zr,Ti)O_3$ ” Physical Review B, **75**, 2007.
- ⁴⁶ J.Shin, J.Park, C-S.Hwang, H-J.Kim. “Dielectric and electrical properties of sputter grown $(Ba,Sr)TiO_3$ thin films” Journal of Applied Physics, **86**, 506, 1999.
- ⁴⁷ J. Sun, X-J. Zheng, W.Yin, M. H. Tang, W. Li. “Space-charge-limited leakage current in high dielectric constant and ferroelectric thin films considering the field-dependent permittivity” Applied Physics letters, **97**, 2010.
- ⁴⁸ S.M.Sze, Physics of Semiconductor Device, 2nd ed. (Wiley, New-York), 1981.
- ⁴⁹ C-J.Peng, S-B.Krupanidhi “Structures and electrical properties of barium strontium titanate thin films grown by multi-ion-beam reactive sputtering technique”, Journal of Materials Research, **10**, pp 708-726, 1995.
- ⁵⁰ T.Baiatu, R.Waser, K-H.Härdt “dc Electrical Degradation of Perovskite-Type Titanates: III, A Model of the Mechanism” Journal of American Ceramic Society, **73**, pp 1663-1673, 1990.
- ⁵¹ R. Bouregba, G. Le Rhun, G. Poullain, G. Leclerc, “Investigation of thickness dependence of the ferroelectric properties of $Pb(Zr_{0.6}Ti_{0.4})$ thin-film capacitors” Journal of Applied Physics, **99**, 034102, 2006.
- ⁵² S.Gevorgian, A.Vorobiev, J.Berge “Electromechanical Modelling and Reduction of the Electroacoustic Losses in Parallel-Plate Ferroelectric Varactors” Proceeding of the 36th European Microwave conference, pp 851-853, 2006.
- ⁵³ K. M. Lakin, G. R. Kline, and K. T. McCarron, “High-Q microwave acoustic resonators and filters,” IEEE Trans. Microw. Theory Tech., **41**, no. 12, pp. 2139–46, 1993.

- ⁵⁴ K. M. Lakin, “Thin film resonator technology,” IEEE Transaction Ultrasonics, Ferroelectrics and Frequency Control, **52**, no. 5, pp. 707–716, 2005.
- ⁵⁵ A. Vorobiev, S. Gevorgian “Composite ferroelectric FBARS that are switchable between the first and second harmonics: experimental demonstration” IEEE Trans. Ultrason., Ferroelect., Freq. Contr., **62**, no. 3, pp. 565–575, 2015.
- ⁵⁶ C. Zhou, D-M. Newns, “Intrinsic dead layer effect and the performance of ferroelectric thin film capacitors” Journal of Applied Physics, **82**, 3081, 1997.
- ⁵⁷ K. Natori, D. Otani, M. Sano, “Thickness dependence of the effective dielectric constant in a thin film capacitor” Applied Physics Letters, **73**, 632, 1998.
- ⁵⁸ M. Grossmann, O. Lohse, D. Bolten, U. Boettger, T. Schneller, R. Waser “Interface-related decrease of the permittivity in $\text{PbZr}_x\text{Ti}_{1-x}\text{O}_3$ thin films” Applied Physics Letters, **80**, 1427, 2002.
- ⁵⁹ J. Junquera, P. Ghosez, “Critical thickness for ferroelectricity in perovskite ultrathin films” Letters to nature, **422**, 506, 2003.
- ⁶⁰ C-S. Hwang, B-T. Lee, C-S. Kang, K-H. Lee, H. Cho, H. Hideki, W-D. Kim, S-I. Lee, M-Y. Lee, “Depletion layer thickness and Schottky type carrier injection at the interface between Pt electrodes and $(\text{Ba}, \text{Sr})\text{TiO}_3$ thin films” Journal of Applied Physics, **85**, 287, 1999.
- ⁶¹ C. Basceri, S-K. Streiffer, A-I. Kingon, R. Waser, “The dielectric response as a function of temperature and film thickness of fiber-textured $(\text{Ba}, \text{Sr})\text{TiO}_3$ thin films grown by chemical vapor deposition” Journal of Applied Physics, **82**, pp 2497-2504, 1997.
- ⁶² A.A. Sirenko, C. Bernhard, A. Golnik, A.M. Clark, J. Hao, W. Si, X. X. Xi “Soft-mode hardening in SrTiO_3 thin films” Letters to nature, **404**, pp 373-376, 2000.
- ⁶³ C-T. Black, J-J. Welser, “Electric-Field Penetration Into Metals: Consequences for High-Dielectric-Constant Capacitors” IEEE Transactions on electronic devices, **46**, pp 776-780, 1999.

